Transient dynamics of terrestrial carbon storage: mathematical foundation and its applications

Yiqi Luo1,2, Zheng Shi1, Xingjie Lu3, Jianyang Xia1, Junyi Liang1, Jiang Jiang1, Ying Wang5, Matthew J. Smith6, Lifen Jiang1, Anders Ahlström7,8, Benito Chen9, Oleksandra Hararuk10, Alan Hastings11, Forrest Hoffman12, Belinda Medlyn13, Shuli Niu14, Martin Rasmussen15, Katherine Todd-Brown16, and Ying-Ping Wang3

1Department of Microbiology and Plant Biology, University of Oklahoma, Norman, Oklahoma, USA
2Department for Earth System Science, Tsinghua University, Beijing, China
3CSIRO Oceans and Atmosphere, Aspendale, Victoria, Australia
4School of Ecological and Environmental Sciences, East China Normal University, Shanghai, China
5Department of Mathematics, University of Oklahoma, Norman, Oklahoma, USA
6Computational Science Laboratory, Microsoft Research, Cambridge, UK
7Department of Earth System Science, Stanford University, Stanford, California, USA
8Department of Physical Geography and Ecosystem Science, Lund University, Lund, Sweden
9Department of Mathematics, University of Texas, Arlington, TX, USA
10Department of Natural Resource Sciences, McGill University, Montreal, Canada
11Department of Environmental Science and Policy, University of California, One Shields Avenue, Davis, CA 95616, USA
12Computational Earth Sciences Group, Oak Ridge National Laboratory, Oak Ridge, TN 37831, USA
13Hawkesbury Institute for the Environment, Western Sydney University, Penrith NSW 2751, Australia
14Institute of Geographic Sciences and Natural Resources Research, Chinese Academy of Sciences, Beijing, China
15Department of Mathematics, Imperial College, London, UK
16Biological Sciences Division, Pacific Northwest National Laboratory, Richland, Washington, USA

Correspondence to: Yiqi Luo (yluo@ou.edu)

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Abstract. Terrestrial ecosystems have absorbed roughly 30% of anthropogenic CO2 emissions over the past decades, but it is unclear whether this carbon (C) sink will endure into the future. Despite extensive modeling and experimental and observational studies, what fundamentally determines transient dynamics of terrestrial C storage under global change is still not very clear. Here we develop a new framework for understanding transient dynamics of terrestrial C storage through mathematical analysis and numerical experiments. Our analysis indicates that the ultimate force driving ecosystem C storage change is the C storage capacity, which is jointly determined by ecosystem C input (e.g., net primary production, NPP) and residence time. Since both C input and residence time vary with time, the C storage capacity is time-dependent and acts as a moving attractor that actual C storage chases. The rate of change in C storage is proportional to the C storage potential, which is the difference between the current storage and the storage capacity. The C storage capacity represents instantaneous responses of the land C cycle to external forcing, whereas the C storage potential represents the internal capability of the land C cycle to influence the C change trajectory in the next time step. The influence happens through redistribution of net C pool changes in a network of pools with different residence times.

Moreover, this and our other studies have demonstrated that one matrix equation can replicate simulations of most land C cycle models (i.e., physical emulators). As a result, simulation outputs of those models can be placed into a three-dimensional (3-D) parameter space to measure their differences. The latter can be decomposed into traceable components to track the origins of model uncertainty. In addition, the physical emulators make data assimilation computation-
ally feasible so that both C flux- and pool-related datasets can be used to better constrain model predictions of land C sequestration. Overall, this new mathematical framework offers new approaches to understanding, evaluating, diagnosing, and improving land C cycle models.

1 Introduction

Terrestrial ecosystems have been estimated to sequester approximately 30% of anthropogenic carbon (C) emissions in the past 3 decades (Canadell et al., 2007). Cumulatively, land ecosystems have sequestered more than 160 Gt C from 1750 to 2015 (Le Quéré et al., 2015). Without land C sequestration, the atmospheric CO$_2$ concentration would have increased by an additional 95 parts per million and resulted in more climate warming (Le Quéré et al., 2015). During 1 decade from 2005 to 2014, terrestrial ecosystems sequestered $3 \pm 0.8$ Gt C year$^{-1}$ (Le Quéré et al., 2015), which would cost 1 billion dollars if the equivalent amount of C was sequestered using C capture and storage techniques (Smith et al., 2016). Thus, terrestrial ecosystems effectively mitigate global change through natural processes with minimal cost. Whether this terrestrial C sequestration will endure into the future, however, is not clear, making the mitigation of global change greatly uncertain. To predict future trajectories of C sequestration in the terrestrial ecosystems, it is essential to understand fundamental mechanisms that drive terrestrial C storage dynamics.

To predict future land C sequestration, the modeling community has developed many C cycle models. According to a review by Manzoni and Porporato (2009), approximately 250 biogeochemical models have been published over a time span of 80 years to describe carbon and nitrogen mineralization. The majority of those 250 models follow some mathematical formulations of ordinary differential equations. Moreover, many of those biogeochemical models incorporate more and more processes in an attempt to simulate C cycle processes as realistically as possible (Oleson et al., 2013). As a consequence, terrestrial C cycle models have become increasingly complicated and less tractable. Almost all model intercomparison projects (MIPs), including those involved in the last three IPCC (Intergovernmental Panel on Climate Change) assessments, indicate that C cycle models have consistently projected widely spread trajectories of land C sinks and were also found to fit observations poorly (Todd-Brown et al., 2013; Luo et al., 2015). The lack of progress in uncertainty analysis urges us to understand the mathematical foundation of those terrestrial C models so as to diagnose causes of model spreads and improve model predictive skills.

Meanwhile, many countries have made great investments on various observational and experimental networks (or platforms) in hope of quantifying terrestrial C sequestration. For example, FLUXNET was established about 20 years ago to quantify net ecosystem exchange (NEE) between the atmosphere and biosphere (Baldocchi et al., 2001). Orbiting Carbon Observatory 2 (OCO-2) satellite was launched in 2014 to quantify carbon dioxide concentrations and distributions in the atmosphere at high spatiotemporal resolution to constrain land surface C sequestration (Hammerling et al., 2012). Networks of global change experiments have been designed to uncover processes that regulate ecosystem C sequestration (Rustad et al., 2001; Luo et al., 2011; Fraser et al., 2013; Borer et al., 2014). Massive data have been generated from those observational systems and experimental networks. They offer an unprecedented opportunity for advancing our understanding of ecosystem processes and constraining model prediction of ecosystem C sequestration. Indeed, many of those networks were initiated with the goal of improving our predictive capability. Yet the massive data have rarely been integrated into earth system models to constrain their predictions. It is a grand challenge in our era to develop innovative approaches to integration of big data into complex models so as to improve prediction of future ecosystem C sequestration.

From a system perspective, ecosystem C sequestration occurs only when the terrestrial C cycle is in a transient state, under which C influx into one ecosystem is larger than C efflux from the ecosystem. Olson (1963) is probably among the first to examine organic matter storage in forest floors from the system perspective. His analysis approximated steady-state storage of organic matter as a balance of litter producers and decomposers for different forest types. However, global change differentially influences various C cycle processes in ecosystems and results in transient dynamics of terrestrial C storage (Luo and Weng, 2011). For example, rising atmospheric CO$_2$ concentration primarily stimulates photosynthetic C uptake, while climate warming likely enhances decomposition. When ecosystem C uptake increases in a unidirectional trend under elevated CO$_2$, terrestrial C cycle is at disequilibrium, leading to net C storage. The net gained C is first distributed to different pools, each of which has a different turnover rate (or residence time) before C is eventually released back to the atmosphere via respiration. Distribution of net C exchange to multiple pools with different residence times is an intrinsic property of an ecosystem to gradually equalize C efflux with influx (i.e., internal recovery force toward an attractor). In contrast, global change factors that cause changes in C input and decomposition are considered external forces that create disequilibrium through altering internal C processes and pool sizes. The transient dynamics of terrestrial C cycle at disequilibrium are maintained by interactions of internal processes and external forces (Luo and Weng, 2011). Although the transient dynamics of terrestrial C storage have been conceptually discussed, we still lack a quantitative formulation to estimate transient C storage dynamics in the terrestrial ecosystems.

This paper was designed to address a question: what determines transient dynamics of C storage in terrestrial ecosys-
tems from a system perspective? We first reviewed the major processes that most models have incorporated to simulate terrestrial C cycle sequestration. The review helps establish that terrestrial C cycle can be mathematically represented by a matrix equation. We also described the Terrestrial ECOsystem (TECO) model with its numerical experiments in support of the mathematical analysis. We then presented results of mathematical analysis on determinants of the terrestrial C storage, direction and magnitude of C storage at a given time point, and numerical experiments to illustrate climate impacts on terrestrial C storage. We carefully discussed assumptions of those terrestrial C cycle models as represented by the matrix equation, the validity of this analysis, and two new concepts introduced in this study, which are C storage capacity and C storage potential. We also discussed the potential applications of this analysis to model uncertainty analysis and data–model integration. Moreover, we proposed that the C storage potential be a targeted variable for research, trading, and government negotiation for C credit.

2 Methods

2.1 Mathematical representation of terrestrial C cycle

This study was conducted mainly with mathematical analysis. We first established the basis of this analysis, which is that the majority of terrestrial C cycle models can be represented by a matrix equation.

Hundreds of models have been developed to simulate terrestrial C cycle (Manzoni and Porporato, 2009). All the models have to simulate processes of photosynthetic C input, C allocation and transformation, and respiratory C loss. It is well understood that photosynthesis is a primary pathway of C flow into land ecosystems. Photosynthetic C input is usually simulated according to carboxylation and electron transport rates (Farquhar et al., 1980). Ecosystem C influx varies with time and space mainly due to variations in leaf photosynthetic capacity, leaf area index of canopy, and a suite of environmental factors such as temperature, radiation, and relative humidity (or other water-related variables) (Potter et al., 1993; Sellers et al., 1996; Keenan et al., 2012; Walker et al., 2014; Parolari and Porporato, 2016).

Photosynthetically assimilated C is partly used for plant biomass growth and partly released back into the atmosphere through plant respiration. Plant biomass in leaves and fine roots usually lives for several months up to a few years before death, while woody tissues may persist for hundreds of years in forests. Dead plant materials are transferred to litter pools and decomposed by microorganisms to be partially released through heterotrophic respiration and partially stabilized to form soil organic matter (SOM). SOM can store C in the soil for hundreds or thousands of years before it is broken down into CO₂ through microbial respiration (Luo and Zhou, 2006). This series of C cycle processes has been represented in most ecosystem models with multiple pools linked by C transfers among them (Jenkinson et al., 1987; Parton et al., 1987, 1988, 1993), including those embedded in Earth system models (Ciais et al., 2013).

The majority of the published 250 terrestrial C cycle models use ordinary differential equations to describe C transformation processes among multiple plant, litter, and soil pools (Manzoni and Porporato, 2009). Those ordinary differential equations can be summarized into a matrix formula (Luo et al., 2001, 2003, 2015, 2016; Luo and Weng, 2011; Sierra and Müller, 2015) as

\[
\begin{align*}
\dot{X}(t) &= BU(t) - AKX(t) \\
X(t) &= X_0
\end{align*}
\]

where \(\dot{X}(t)\) is a vector of net C pool changes at time \(t\), \(X(t)\) is a vector of pool sizes, \(B\) is a vector of partitioning coefficients from C input to each of the pools, \(u(t)\) is C input rate, \(A\) is a matrix of transfer coefficients (or microbial C use efficiency) to quantify C movement along the pathways, \(K\) is a diagonal matrix of exit rates (mortality for plant pools and decomposition coefficients of litter and soil pools) from donor pools, \(\xi(t)\) is a diagonal matrix of environmental scalars to represent responses of C cycle to changes in temperature, moisture, nutrients, litter quality, and soil texture, and \(X_0\) is a vector of initial values of pool sizes of \(X\). In Eq. (1), all the off-diagonal elements of matrix \(A\), \(a_{ji}\), are negative to reverse the minus sign and indicate positive C influx to the receiving pools. The equation describes net C pool change, \(\dot{X}(t)\), as a difference between C input, \(u(t)\), distributed to different plant pools via partitioning coefficients, \(B\), and C loss through the C transformation matrix, \(AK\), among individual pools, \(X(t)\). Elements in vector \(B\) and matrices \(A\) and \(K\) could vary with many factors, such as vegetation types, soil texture, microbial attributes, and litter chemistry. For example, vegetation succession may influence elements in vector \(B\) and matrices \(A\) and \(K\) in addition to C input, \(u(t)\), and forcing that affects C dynamics through environmental scalars, \(\xi(t)\).

After synthesis of all the possible soil C cycle models based on six principles (mass balance, substrate dependence of decomposition, heterogeneity of decay rates, internal transformations of organic matter, environmental variability effects, and substrate interactions), Sierra and Müller (2015) concluded that this form of matrix equation such as Eq. (1) represents the majority of terrestrial C cycle models. Similarly, Manzoni and Porporato (2009) concluded in their review of 250 models that the majority of them use ordinary differential equations, which can be summarized by Eq. (1), to describe land C cycle. Our mathematical analysis in this study used matrix operations of Eq. (1) to reveal determinants of transient dynamics of the terrestrial C cycle, including direction and rate of C storage changes, in response to global change. We examined assumptions underlying this equation and the validity of our analysis in the discussion section.
2.2 TECO model, its physical emulator, and numerical experiments

We conducted numerical experiments to support mathematical analysis and thus help understand the characteristics of terrestrial C storage dynamics using the Terrestrial ECOsystem (TECO) model. TECO has five major components: canopy photosynthesis, soil water dynamics, plant growth, litter and soil carbon decomposition and transformation, and nitrogen dynamics, as described in detail by Weng and Luo (2008) and Shi et al. (2016). Canopy photosynthesis is from a two-leaf (sunlit and shaded) model developed by Wang and Leuning (1998). This submodel simulates canopy conductance, photosynthesis, and partitioning of available energy. The model combines the leaf photosynthesis model developed by Farquhar et al. (1980) and a stomatal conductance model (Harley et al., 1992). In the soil water dynamic submodel, soil is divided into 10 layers. The surface layer is 10 cm deep and the other nine layers are 20 cm deep. Soil water content (SWC) in each layer results from the mass balance between water influx and efflux. The plant growth submodel simulates C allocation and phenology. Allocation of C among three plant pools, which are leaf, fine root, and wood, depends on their growth rates (Fig. 1a). Phenology dynamics is related to leaf onset, which is triggered by growing degree days, and leaf senescence, which is determined by temperature and soil moisture. The C transformation submodel estimates carbon transfer from plants to two litter pools and three soil pools (Fig. 1a). The nitrogen (N) submodel is fully coupled with C processes with one additional mineral N pool. Nitrogen is absorbed by plants from mineral soil and then partitioned among leaf, woody tissues, and fine roots. Nitrogen in plant detritus is transferred among different ecosystem pools (i.e., litter, coarse wood debris, and fast, slow, and passive SOM) (Shi et al., 2016). The model is driven by climate data, which include air and soil temperature, vapor-pressure deficit, relative humidity, incident photosynthetically active radiation, and precipitation at hourly steps.

We first calibrated TECO with eddy flux data collected at Harvard Forest from 2006–2009. The calibrated model was spun up to the equilibrium state in preindustrial environmental conditions by recycling a 10-year climate forcing (1850–1859). Then the model was used to simulate C dynamics from 1850 to 2100 with the historical forcing scenario for 1850–2005 and RCP8.5 scenario for 2006–2100 as in the Community Land Model 4.5 (Oleson et al., 2013) in the grid cell where Harvard Forest is located.

To support the mathematical analysis using Eq. (1), we first developed a physical emulator (i.e., the matrix representation of Eq. 1) of the TECO model and then verified that the physical emulator can closely represent simulations of the original TECO model. We first identified those parame-
ter values in each of the C balance equations in the TECO model that correspond to elements in matrices $A$ and $K$ in Eq. (1). The time-dependent variables for $u(t)$, elements in vector $B$, and elements in matrix $\xi(t)$ in the physical emulator were directly from outputs of the original TECO model. Then those parameter values and time-dependent variables were organized into matrices $A$, $\xi(t)$, and $K$; vectors $X(t)$, $X_0$, and $B$; and variable $u(t)$. Note that values of $u(t)$, $B$, and $\xi(t)$ could be different among different climate scenarios. Those matrices, vectors, and variables were entered to matrix calculation to compute $X'(t)$ using Eq. (1). The sum of elements in calculated $X'(t)$ is a 100\% match with simulated net ecosystem production (NEP) with the TECO model (Fig. 1b).

Once Eq. (1) was verified to exactly replicate TECO simulations, we used TECO to generate numerical experiments to support the mathematical analysis of the transient dynamics of terrestrial C storage. To analyze the seasonal patterns of C storage dynamics, we averaged 10 series of 3-year seasonal dynamics from 1851–1880. Then we used a 7-day moving window to further smooth the data.

3 Results

3.1 Determinants of C storage dynamics

The transient dynamics of terrestrial carbon storage are determined by two components: the C storage capacity and the C storage potential. The two components of C storage dynamics can be mathematically derived by multiplying both sides of Eq. (1) by $(A\xi(t)K)^{-1}$ as

$$X(t) = (A\xi(t)K)^{-1}Bu(t) - (A\xi(t)K)^{-1}X'(t).$$

The first term on the right-hand side of Eq. (2) is the C storage capacity and the second term is the C storage potential. Figure 2a shows time courses of C storage and its capacity over 1 year for the leaf pool of Harvard Forest.

In Eq. (2), we name the term $(A\xi(t)K)^{-1}$ the chasing time, $\tau_{ch}(t)$, with a time unit used in exit rate $K$. The chasing time is defined as

$$\tau_{ch}(t) = (A\xi(t)K)^{-1}.$$  

$\tau_{ch}(t)$ is a matrix of C residence times through the network of individual pools, each with a different residence time and fractions of received C connected by pathways of C transfer. Analogous to the fundamental matrix measuring life expectancies in demographic models (Caswell, 2000), the matrix, $\tau_{ch}(t)$, measures expected residence time of a C atom in pool $i$ when it has entered from pool $j$. We call this matrix the fundamental matrix of chasing times to represent the timescale at which the net C pool change, $X'(t)$, is redistributed in the network. Meanwhile, the residence times of individual pools in the network, $\tau_N(t)$, can be estimated by multiplying the fundamental matrix of chasing times, $(A\xi(t)K)^{-1}$, with a vector of partitioning coefficients, $B$, as

$$\tau_N(t) = (A\xi(t)K)^{-1}B.$$  

Ecosystem residence time, $\tau_E(t)$, is the sum of the residence time of all individual pools in the network as

$$\tau_E(t) = (1\ 1\ \ldots\ 1)\tau_N(t).$$

Thus, the C storage capacity can be defined by

$$X_c(t) = (A\xi(t)K)^{-1}Bu(t).$$

Alternatively, it can be estimated from C input, $u(t)$, and residence time, $\tau_N(t)$, as

$$X_c(t) = \tau_N(t)u(t).$$

As C input (e.g., gross or net primary productions, GPP or NPP) and residence times vary with time, the C storage capacity varies with time. It represents instantaneous responses of the terrestrial C cycle to external forcing. The modeled C storage capacity in the leaf pool (Fig. 2a), for example, increases in spring, reaches the peak in summer, declines in autumn, and becomes minimal in winter, largely due to strong seasonal changes in C input (Fig. 2b). Note that either GPP or NPP can be used as C input for analysis of transient C dynamics. Estimated residence times, however, are smaller with GPP as C input than those with NPP as input. In this paper, we mostly used NPP as C input since that fraction of C is distributed among pools.

Figure 2. Seasonal cycles of C storage capacity and C storage dynamics for the leaf pool (i.e., pool 1 as shown in Fig. 1). All the components are shown in panels (b–d) to calculate $X_{c,1}(t) = b_1u(t)\tau_1$ through multiplication, where $u(t) = \text{NPP}$ and $\tau_1 = 1/k_1$ for leaf.
The C storage potential at time \( t \), \( X_p(t) \), can be mathematically described as
\[
X_p(t) = (A\xi(t)K)^{-1}X'(t).
\]
(6a)

Or it can be estimated from net C pool change, \( X'(t) \), and chasing time, \( \tau_{ch} \) as
\[
X_p(t) = \tau_{ch}X'(t).
\]
(6b)

Equation (6a) and (6b) suggest that the C storage potential represents redistribution of net C pool change, \( X'(t) \), of individual pools through a network of pools with different residence times as connected by C transfers from one pool to the others through all the pathways. As time evolves, the net C pool change, \( X'(t) \), is redistributed again and again through the network of pools. The network of redistribution of the next C pool change thus represents the potential of an ecosystem to store additional C when it is positive and lose C when it is negative. The C storage potential can also be estimated from the difference between the C storage capacity and the C storage itself at time \( t \) as
\[
X_p(t) = X_c(t) - X(t).
\]
(6c)

The C storage potential in the leaf pool, for example, is about zero in winter and early spring when the C storage capacity is very close to the storage itself (Fig. 2a). The C storage potential is positive when the capacity is larger than the storage itself from late spring to summer and early fall. As the storage capacity decreases to the point when the storage equals the capacity on the 265th day of the year (DOY), the C storage potential is zero. After that day, the C storage potential becomes negative.

Dynamics of ecosystem C storage, \( X(t) \), can be characterized by three parameters: C influx, \( u(t) \), residence times, \( \tau_N(t) \), and the C storage potential, \( X_p(t) \), as
\[
X(t) = \tau_N(t)u(t) - X_p(t).
\]
(7)

Equation (7) represents a three-dimensional (3-D) parameter space within which model simulation outputs can be placed to measure how and how much they diverge.

Note that sums of elements of vectors \( X(t) \), \( X_c(t) \), \( X_p(t) \), and \( X'(t) \) correspond, respectively, to the whole ecosystem C stock, ecosystem C storage capacity, ecosystem C storage potential, and NEP. In this paper, we describe them wherever necessary rather than use a separate set of symbols to represent those sums.

3.2 Direction and rate of C storage change at a given time

Like studying any moving object, quantifying dynamics of land C storage needs to determine both the direction and the rate of its change at a given time. To determine the direction and rate of C storage change, we rearranged Eq. (2) to be
\[
\tau_{ch}X'(t) = X_c(t) - X(t) = X_p(t),
\]
(8a)
or rearranging Eq. (6a) leads to
\[
X'(t) = A\xi(t)KX_p(t).
\]
(8b)

Since all the elements in \( \tau_{ch} \) are positive, the sign of \( X'(t) \) is the same as for \( X_p(t) \). That means that \( X'(t) \) increases when \( X_c(t) > X(t) \), does not change when \( X_c(t) = X(t) \), and decreases when \( X_c(t) < X(t) \) at the ecosystem scale. Thus, the C storage capacity, \( X_c(t) \), is an attractor and hence determines the direction toward which the C storage, \( X(t) \), chases at any given time point. The rate of C storage change, \( X'(t) \), is proportional to \( X_p(t) \) and is also regulated by \( \tau_{ch} \).

When we study C cycle dynamics, we are interested in understanding dynamics of not only a whole ecosystem but also individual pools. Equation (8a) can be used to derive equations to describe C storage change for an \( i \)th pool as
\[
\sum_{j=1}^{n} f_{ij} \tau_j x_j' = \sum_{j=1}^{n} f_{ij} \tau_j b_j u(t) - x_i(t) = x_{p,i}(t),
\]
(9a)

where \( n \) is the number of pools in a C cycle model, \( f_{ij} \) is a fraction of C transferred from pool \( j \) to \( i \) through all the pathways, \( \tau_i \) measures residence times of individual pools in isolation (in contrast to \( \tau_N \) in the network), \( x_j' \) is the net C change in the \( j \)th pool, \( b_j \) is a partitioning coefficient of C input to the \( j \)th pool, \( x_i(t) \) is the C storage in the \( i \)th pool, and \( x_{p,i}(t) \) is the C storage potential in the \( i \)th pool. Equation (9a) means that the C storage potential of each pool at time \( t \), \( x_{p,i}(t) \), is the sum of all the individual net C pool change, \( x_j' \), multiplied by corresponding residence time spent in pool \( j \) coming from pool \( i \). Through rearrangement, Eq. (9a) can be solved for each individual pool net C change as a function of C storage potential of all the pools as
\[
x_j'(t) = \frac{x_{c,j,u}(t) - x_{c,j,p}(t)}{f_{ii} \tau_i} - x_i(t).
\]
(9b)

where \( x_{c,j,u}(t) = \sum_{j=1}^{n} f_{ij} \tau_j b_j u(t) \) for the maximal amount of C that can transfer from C input to the \( i \)th pool. \( x_{c,j,p}(t) = \sum_{j=1, j \neq i}^{n} f_{ij} \tau_j x_j' \) for the maximal amount of C that can transfer from all the other pools to the \( i \)th pool. \( f_{ii} = 1 \) for all the pools if there is no feedback of C among soil pools. \( f_{ii} < 1 \) when there are feedbacks of C among soil pools.

As plant pools get C only from photosynthetic C input, \( u(t) \), but not from other pools, the direction and rate of C storage change in the \( i \)th plant pool is determined by
\[
\begin{aligned}
x_i'(t) &= \frac{x_{c,i}(t)}{\tau_i} - x_i(t) = \frac{X_{p,i}(t)}{\tau_i} \quad \text{for } i = 1, 2, 3.
\end{aligned}
\]
(10)

The C storage capacity of plant pools equals the product of plant C input, \( u(t) \) (i.e., net primary production, NPP), partitioning coefficient, \( b_i \), and residence time, \( \tau_i \), of its own
The capacities for individual litter and soil pools measure the amount of C that is transferred from photosynthetic C input through all the possible pathways, multiplying net C pool change in those pools. Integration of C input and C exchanges together is still a moving attractor toward which individual pool C storage approaches (Fig. 4).

In summary, due to the network of C transfer, C storage in litter and soil pools does not chase the C storage capacities of their own pools in a multiple C pool model (Fig. 4). The capacities for individual litter and soil pools measure the amount of C that is transferred from photosynthetic C input through all the possible pathways, multiplying net C pool change in those pools. Integration of C input and C exchanges together is still a moving attractor toward which individual pool C storage approaches (Fig. 4).

3.3 C storage dynamics under global change

In response to a global change scenario that combines historical change and simulated RCP8.5 in the TECO experiment, the modeled ecosystem C storage capacity (the sum of all elements in vector \( X_c(t) \)) at Harvard Forest increases from
Figure 4. Components of the C storage capacity for litter pool (i.e., pool 4 as shown in Fig. 1). Component $x_{c, 4,u}(t)$ is the C from C input and component $x_{c, 4,p}(t)$ is the C moved from all the other pools to the litter pool. The sum of them is the attractor that determines the direction of C storage change in pool 4.

27 kg C m\(^{-2}\) in 1850 to approximately 38 kg C m\(^{-2}\) in 2100 with strong interannual variability (Fig. 5a). The increasing capacity results from a combination of a nearly 44 % increase in NPP with a ~ 2 % decrease in ecosystem residence times (the sum of all elements in vector $\tau_E(t)$) during that period (Fig. 5b). The strong interannual variability in the modeled capacity is attributable to the variability in NPP and residence times, both of which directly respond to instantaneous variations in environmental factors. In comparison, the ecosystem C storage (the sum of all elements in vector $X(t)$) itself gradually increases, lagging behind the capacity, with much dampened interannual variability (Fig. 5a). The dampened interannual variability is due to smoothing effects of pools with various residence times. In response to global change scenario RCP8.5, the ecosystem C storage potential (the sum of all elements in vector $X_p(t)$) in the Harvard Forest ecosystem increases from zero at 1980 to 3.5 kg C m\(^{-2}\) in 2100 with strong fluctuation over the years (Fig. 5a). Over seasons, the potential is high during the summer and low in winter, similar to the seasonal cycle of the C storage capacity.

Since chasing time, $\tau_{ch}$, is a matrix and net C pool change, $X'(t)$, is a vector, Eq. (6a) or (6b) (i.e., the C storage potential) can not be analytically separated into the chasing time and net C pool change as the capacity can be into C input and residence time in Eq. (5a) or (5b) for traceability analysis. The relationships among the three quantities can be explored using regression analysis. The ecosystem C storage potential fluctuates in a similar phase with NEP from 1850 to 2100 (Fig. 5c). Consequently, the C storage potential is well correlated with NEP at the whole ecosystem scale (Fig. 5d). The slope of the regression line is a statistical representation of ecosystem chasing time. In this study, we find that $r^2$ of the relationship between the storage potential and NEP is 0.79. The regression slope is 28.1 years in comparison with the ecosystem residence time of approximately 22 years (Fig. 5b).

The capacity and storage of individual pools display similar long-term trends and interannual variability to those for the total ecosystem C storage dynamics (Fig. 6). Noticeably, the deviation of the C storage from the capacity, which is the C storage potential, is much larger for pools with long residence times than those with short residence times. For individual pools, the potential is nearly zero for those fast turnover pools and becomes very large for those pools with a long residence time (Fig. 6).

For individual plant pools, Eq. (10) describes the dependence of the C storage potential, $x_{p,i}(t)$, on the pool-specific residence time, $\tau_{i}, i = 1, 2, \text{ and } 3$, and net C pool change of their own pools, $x_{p,i}'(t), i = 1, 2, \text{ and } 3$. Thus, one value of $x_{p,i}(t)$ corresponds exactly to one value of $x_{p,i}'(t)$ at slope of $\tau_{i}$, leading to a correlation coefficient in Fig. 7 of 1.00 for leaf, root, and wood pools. For a litter or soil pool, however, the C storage potential is not solely dependent on the residence time and net C pool change of its own pool but is influenced by several other pools. Thus, the potential of one litter or soil pool is correlated with net C pool changes of several pools with different regression slopes (Fig. 7).
Figure 6. The C storage capacity \( (x_{c,i}(t)) \), the C storage potential \( (x_{p,i}(t)) \), and C storage \( (x_i(t)) \) of individual pools. The potential is nearly zero for those fast turnover pools with short residence times but very large for those pools with long residence times.

Figure 7. The C storage potential of individual pools \( (x_{p,i}) \) as influenced by net C pool change of different pools \( (x'_i) \) in their corresponding rows. The correlation coefficients show the degree of influence of net C pool change in one pool on the C storage potential of the corresponding pool through the network of C transfer. The empty cells indicate no pathways of C transfer between those pools as indicated in Fig. 1.

4 Discussion

4.1 Assumptions of the C cycle models and validity of this analysis

This analysis is built upon Eq. (1), which represents the majority of terrestrial C cycle models developed in the past decades (Manzoni and Porporato, 2009; Sierra and Müller, 2015). These models have several assumptions, which may influence the validity of this analysis. First, these models assume that donor pools control C transfers among pools and decomposition follows first-order decay functions (assumption 1). This assumption is built upon observations from litter and SOC decomposition. Analysis of data from nearly 300 studies of litter decomposition (Zhang et al., 2008), about 500 studies of soil incubation (Schädel et al., 2014; Xu et al., 2016), more than 100 studies of forest succession (Yang et al., 2011), and restoration (Matamala et al., 2008) almost all suggests that the first-order decay function captures macroscopic patterns of land C dynamics. Even so, its biological, chemical, and physical underpinnings need more study (Luo et al., 2016). This assumption has recently been challenged by a notion that microbes are actively involved in decomposition processes. To describe the active roles of microbes in organic C decomposition, a suite of nonlinear microbial models has been proposed using Michaelis–Menten or reverse Michaelis–Menten equations (Allison et al., 2010; Wieder et al., 2013). Those nonlinear models exhibit unique behaviors of modeled systems, such as damped oscillatory responses of soil C dynamics to small perturbations and insensitivity of the equilibrium pool sizes of litter or soil carbon to inputs (Li et al., 2014; Wang et al., 2014, 2016). Oscillations have been documented for single enzymes at timescales between \( 10^{-4} \) and 10 s (English et al., 2006; Goldbeter, 2013; Xie, 2013). Over longer timescales with largely diverse mixtures of enzyme-substrate complexes in soil, oscillations may be likely averaged out so that the first-order decay functions may well approximate these average dynamics of organic matter decomposition (Sierra and Müller, 2015).
Second, those models all assume that multiple pools can adequately approximate transformation, decomposition, and stabilization of SOC in the real world (assumption 2). The classic SOC model, CENTURY, uses three conceptual pools, active, slow, and passive SOC, to represent SOC dynamics (Parton et al., 1987). Several models define pools that correspond to measurable SOC fractions to match experimental observation with modeling analysis (Smith et al., 2002; Stewart et al., 2008). Carbon transformation in soil over time has also been described by a partial differential function of SOM quality (Bosatta and Ågren, 1991; Ågren and Bosatta, 1996). The latter quality model describes the external inputs of C with certain quality, C loss due to decomposition, and the internal transformations of the quality of soil organic matter. It has been shown that multi-pool models can approximate the partial differential function or continuous quality model as the number of pools increases (Bolker et al., 1998; Sierra and Müller, 2015).

Assumption 3 is on partitioning coefficients of C input (i.e., elements in vector $B$) and C transformation among plant, litter, and soil pools (i.e., elements in the matrix $A$). Some of the terrestrial C cycle models assume that elements in vector $B$ and matrices $A$ and $K$ are constants. All the factors or processes that vary with time are represented in the diagonal matrix $\xi(t)$. In the real world, C transformation is influenced by environmental variables (e.g., temperature, moisture, oxygen, N, phosphorus, and acidity varying with soil profile, space, and time), litter quality (e.g., lignin, cellulose, N, or their relative content), organomineral properties of SOC (e.g., complex chemical compounds, aggregation, physiochemical binding and protection, reactions with inorganic, reactive surfaces, and sorption), and microbial attributes (e.g., community structure, functionality, priming, acclimation, and other physiological adjustments) (Luo et al., 2016). It is not practical to incorporate all of those factors and processes into one model. Only a subset of them is explicitly expressed, while the majority is implicitly embedded in the C cycle models. Empirical studies have suggested that temperature, moisture, litter quality, and soil texture are primary factors that control C transformation processes of decomposition and stabilization (Burke et al., 1989; Adair et al., 2008; Zhang et al., 2008; Xu et al., 2012; Wang et al., 2013). Nitrogen influences C cycle processes mainly through changes in photosynthetic C input, C partitioning, and decomposition. It is yet to be identified how other major factors and processes, such as microbial activities and organomineral protection, regulate C transformation.

Assumption 4 is that terrestrial C cycle models use different response functions (i.e., different $\xi(t)$ in Eq. 1) to represent C cycle responses to external variables. As temperature modifies almost all processes in the C cycle, different formulations, including exponential, Arrhenius, and optimal response functions, have been used to describe C cycle responses to temperature changes in different models (Lloyd and Taylor, 1994; Jones et al., 2005; Sierra and Müller, 2015). Different response functions are used to connect C cycle processes with moisture, nutrient availability, soil clay content, litter quality, and other factors. Different formulations of response functions may result in substantially different model projections (Exbrayat et al., 2013) but are unlikely to change basic dynamics of the model behaviors.

Assumption 5 is that disturbance events are represented in models in different ways (Grosse et al., 2011; West et al., 2011; Goetz et al., 2012; Hicke et al., 2012). Fire, extreme drought, insect outbreaks, land management, and land cover and land use change influence terrestrial C dynamics via (1) altering rate processes, for example, gross primary productivity (GPP), growth, tree mortality, or heterotrophic respiration; (2) modifying microclimatic environments; or (3) transferring C from one pool to another (e.g., from live to dead pools during storms or release to the atmosphere with fire) (Kloster et al., 2010; Thonicke et al., 2010; Luo and Weng, 2011; Prentice et al., 2011; Weng et al., 2012). Those disturbance influences can be represented in terrestrial C cycle models through changes in parameter values, environmental scalars, and/or discrete C transfers among pools of Eq. (1) (Luo and Weng, 2011). While Eq. (1) does not explicitly incorporate disturbances for their influences on land C cycle, Weng et al. (2012) developed a disturbance regime model that combines Eq. (1) with frequency distributions of disturbance severity and intervals to quantify net biome exchanges.

The sixth assumption that those models make is that the lateral C fluxes through erosion or local C drainage are negligible so that Eq. (1) can approximate terrestrial C cycle over space. If soil erosion is substantial enough to be modeled with horizontal movement of C, a third dimension should be added in addition to two-dimensional transfers in classic models.

Our analysis on transient dynamics of terrestrial C cycle is valid unless some of the assumptions are violated. Assumption 1 on the first-order decay function of decomposition appears to be supported by thousands of datasets. It is a burden on microbiologists to identify empirical evidence to support the nonlinear microbial models. Assumption 2 may not affect the validity of our analysis no matter how C pools are divided in the ecosystems. Our analysis in this study is applicable no matter whether elements are time-varying or constant in vector $B$ and matrices $A$ and $K$ as in assumption 3. Neither assumption 4 nor 5 would affect the analysis in this study. The environmental scalar, $\xi(t)$, as related to assumption 4 can be any forms in the derived equations (e.g., Eq. 2). Disturbances of fire, land use, and extreme drought change rate processes but do not alter the basic formulation of Eq. (1). If soil erosion and lateral transportation of C become major research objectives, Eq. (1) can no longer be analyzed to understand the mathematical foundation underlying transient dynamics of terrestrial C cycle.
4.2 Carbon storage capacity

One of the two components this analysis introduces to understand transient dynamics of terrestrial C storage is the C storage capacity (Eq. 2). Olson (1963) is probably among the first who systematically analyzed C storage dynamics at the forest floor as functions of litter production and decomposition. He collected data of annual litter production and approximately steady-state organic C storage at the forest floor, from which decomposition rates were estimated for a variety of ecosystems from Ghana in the tropics to alpine forests in California. Using the relationships among litter production, decomposition, and C storage, Olson (1963) explored several issues, such as decay without input, accumulation with continuous or discrete annual litter fall, and adjustments in production and decay parameters during forest succession. His analysis approximated the steady-state C storage as the C input times the inverse of decomposition (i.e., residence time). The steady-state C storage is also considered the maximal amount of C that a forest can store.

This study is not only built upon Olson’s analysis but also expands it in at least two aspects. First, we similarly define the C storage capacity (i.e., Eq. 5a and 5b). Those equations can be applied to a whole ecosystem with multiple C pools, while Olson’s analysis is for one C pool. Second, Olson (1963) treated the C input and decomposition rate as yearly constants at a given location even though they varied with locations. This study considers both C input and rate of decomposition being time dependent. A dynamical system with its input and parameters being time dependent mathematically becomes a nonautonomous system (Kloeden and Rasmussen, 2011). As terrestrial C cycle under global change is transient, we need to treat it as a nonautonomous system to better understand the properties of transient dynamics. Olson (1963) approximated the nonautonomous system at the yearly timescale without global change so as to effectively understand properties of steady-state C storage at the forest floor. In comparison, Eq. (5a) and (5b) are not only more general but also essential for understanding transient dynamics of the terrestrial C cycle in response to global change.

Under the transient dynamics, the C storage capacity as defined by Eq. (5a) and (5b) still sets the maximal amount of C that one ecosystem can store at time \( t \). This capacity represents instantaneous responses of ecosystem C cycle to external forcing via changes in both C input and residence time, and thus varies within 1 day, over seasons of a year, and interannually over longer timescales as forcings vary. The variation of the C storage capacity can result from cyclic environmental changes (e.g., dial and seasonal changes), directional global change (e.g., rising atmospheric CO\(_2\), nitrogen deposition, altered precipitation, and warming), disturbance events, disturbance regime shifts, and changing vegetation dynamics (Luo and Weng, 2011). Since the capacity sets the maximal amount of C storage (Fig. 2a), it is a moving attractor toward which the current C storage chases. When the capacity is larger than the C storage itself, C storage increases. Otherwise, the C storage decreases.

4.3 Carbon storage potential

The C storage potential represents the internal capability to equilibrate the current C storage with the capacity. Biogeochemically, the C storage potential represents redistribution of net C pool change, \( X'(t) \), of individual pools through a network of pools with different residence times as connected by C transfers from one pool to the others through all the pathways. The potential is conceptually equivalent to the magnitude of disequilibrium as discussed by Luo and Weng (2011).

Extensive studies have been done to quantify terrestrial C sequestration. The most commonly estimated quantities for C sequestration include net ecosystem exchange (NEE) and C stocks in ecosystems (i.e., plant biomass and SOC) and their changes (Baldocchi et al., 2001; Pan et al., 2013). This study, for the first time, offers the theoretical basis to estimate the terrestrial C storage potential in at least two approaches: (1) the product of chasing time and net C pool change with Eq. (6a) and (6b) and (2) the difference between the C storage capacity and the C storage itself with Eq. (6c). Since the time-varying C storage capacity is fully defined by residence time and C input at any given time, C storage potential can be estimated from three quantities: C input, residence time, and C storage.

To effectively quantify the C storage potential in terrestrial ecosystems, we need various datasets from experimental and observatory studies to be first assimilated into models. For example, data from Harvard Forest were first used to constrain the TECO model. The constrained model was used to explore changes in ecosystem C storage in response to global change scenario, RCP8.5. That scenario primarily stimulated NPP, which increased from 1.06 to 1.8 kg C m\(^{-2}\) yr\(^{-1}\) in the Harvard Forest (Fig. 5b). Although climate warming decreased ecosystem C residence time in the Harvard Forest, the substantial increases in NPP resulted in increases in the C storage potential over time.

4.4 Novel approaches to model evaluation and improvement

Our analysis of transient C cycle dynamics offers new approaches to understand, evaluate, diagnose, and improve land C cycle models. We have demonstrated that many global land C cycle models can be exactly represented by the matrix equation (Eqs. 1 and 2) (i.e., physical emulators). As a consequence, outputs of all those models can be placed into a three dimensional (3-D) space (Eq. 7) to measure their differences. In addition, components of land C cycle models are simulated in a mutually independent fashion so that modeled C storage can be decomposed into traceable components for traceability analysis. Moreover, the physical emulators com-
putationally enable data assimilation to constrain complex models.

4.4.1 Physical emulators of land C cycle models

We have developed matrix representations (i.e., physical emulators) of CABLE, LPJ-GUESS, CLM3.5, CLM4.0, CLM4.5, BEPS, and TECO (Xia et al., 2013; Hararuk et al., 2014; Ahlström et al., 2015; Chen et al., 2015). The emulators can exactly replicate simulations of C pools and fluxes with their original models when driven by a limited set of inputs from the full model (GPP, soil temperature, and soil moisture) (Fig. 1b and c). However, the physical emulators differ for different models since the elements of each matrix could be differently parameterized or formulated in different models. Also, different models usually have different pool-flux structures, leading to different non-zero elements in the $A$ matrix. Nonetheless, the physical emulators make complex models analytically clear, and therefore give us a way to understand the effects of forcing, model structures, and parameters on modeled ecosystem processes. They greatly simplify the task of understanding the dynamics of submodels and interactions between them. The emulators allow us to analyze model results in the 3-D parameter space and the traceability framework.

4.4.2 Parameter space of C cycle dynamics

Equation (7) indicates that transient dynamics of modeled C storage are determined by three parameters: C input, residence time, and C storage potential. The 3-D parameter space offers a novel approach to uncertainty analysis of global C cycle models. As global land models incorporate more and more processes to simulate C cycle responses to global change, it becomes very difficult to understand or evaluate complex model behaviors. As such, differences in model projections cannot be easily diagnosed and attributed to their sources (Chatfield, 1995; Friedlingstein et al., 2006; Luo et al., 2009). Equation (7) can help diagnose and evaluate complex models by placing all modeling results within one common parameter space in spite of the fact that individual global models may have tens or hundreds of parameters to represent C cycle processes as affected by many abiotic and biotic factors (Luo et al., 2016). The 3-D space can be used to measure how and how much the models diverge.

4.4.3 Traceability analysis

The two terms on the right side of Eq. (2) can be decomposed into traceable components (Xia et al., 2013) so as to identify sources of uncertainty in C cycle model projections. Model intercomparison projects (MIPs) all illustrate great spreads in projected land C sink dynamics across models (Todd-Brown et al., 2013; Tian et al., 2015). It has been extremely challenging to attribute the uncertainty to sources. Placing simulation results of a variety of C cycle models within one common parameter space can measure how much the model differences are in a common metric (Eq. 7). The measured differences can be further attributed to sources in model structure, parameter, and forcing fields with traceability analysis (Xia et al., 2013; Rafique et al., 2014; Ahlström et al., 2015; Chen et al., 2015). The traceability analysis can also be used to evaluate effectiveness of newly incorporated modules into existing models, such as adding the N module on simulated C dynamics (Xia et al., 2013) and locate the origin of model ensemble uncertainties to external forcing vs. model structures and parameters (Ahlström et al., 2015).

4.4.4 Constrained estimates of terrestrial C sequestration

Traditionally, global land C sink is indirectly estimated from airborne fraction of C emission and ocean uptake. Although many global land models have been developed to estimate land C sequestration, a variety of MIPs indicate that model predictions widely vary among them and do not fit observations well (Schwalm et al., 2010; Luo et al., 2015; Tian et al., 2015). Moreover, the prevailing practices in the modeling community, unfortunately, may not lead to significant enhancements in our confidence on model predictions. For example, incorporating an increasing number of processes that influence the C cycle may represent the real-world phenomena more realistically but makes the models more complex and less tractable. MIPs have effectively revealed the extent of the differences between model predictions (Schwalm et al., 2010; Keenan et al., 2012; De Kauwe et al., 2013) but provide limited insights into sources of model differences (see Medlyn et al., 2015). The physical emulators make data assimilation computationally feasible for global C cycle models (Hararuk et al., 2014, 2015) and thus offer the possibility to generate independent yet constrained estimates of global land C sequestration to be compared with the indirect estimate from the airborne fraction of C emission and ocean uptake. With the emulators, we can assimilate most of the C flux- and pool-related datasets into those models to better constrain global land C sink dynamics.

5 Concluding remarks

In this study we theoretically explored the transient dynamics of terrestrial C storage. Our analysis indicates that transient C storage dynamics can be partitioned into two components: the C storage capacity and the C storage potential. The capacity, which is the product of C input and residence time, represents their instantaneous responses to a state of external forcing at a given time. Thus, the C storage capacity quantifies the maximum amount of C that an ecosystem can store at the given environmental condition at a point of time. Thus, it varies diurnally, seasonally, and interannually as environmental conditions change.
The C storage potential is the difference between the capacity and the current C storage and thus measures the magnitude of disequilibrium in the terrestrial C cycle (Luo and Weng, 2011). The storage potential represents the internal capability (or recovery force) of the terrestrial C cycle to influence the change in C storage in the next time step through redistribution of net C pool changes in a network of multipool systems with different residence times. The redistribution drives the current C storage towards the capacity and thus equilibrates C efflux with influx.

The two components of land C storage dynamics represent interactions of external forces (via changes in the capacity) and internal capability of the land C cycle (via changes in the C storage potential) to generate complex phenomena of C cycle dynamics, such as fluctuations, directional changes, and tipping points, in the terrestrial ecosystems. From a system perspective, these complex phenomena can not be generated by relatively simple internal processes but are mostly caused by multiple environmental forcing variables interacting with internal processes over different temporal and spatial scales, as explained by Luo and Weng (2011) and Luo et al. (2015). Note that while those internal processes can be mathematically represented with a relatively simple formula, their ecological and biological underpinnings can be very complex.

The theoretical framework developed in this study has the potential to revolutionize model evaluation. Our analysis indicates that the matrix equation as in Eqs. (1) and (2) can adequately emulate most of the land C cycle models. Indeed, we have developed physical emulators of several global land C cycle models. In addition, predictions of C dynamics with complex land models can be placed in a 3-D parameter space as a common metric to measure how much model predictions are different. The latter can be traced to its source components by decomposing model predictions to a hierarchy of traceable components. Moreover, the physical emulators make it computationally possible to assimilate multiple sources of data to constrain predictions of complex models.

The theoretical framework we developed in this study can explain dynamics of C storage in response to cyclic seasonal change in external forcings (e.g., Figs. 2 and 3), climate change, and rising atmospheric CO₂ well (Fig. 5). It can also explain responses of ecosystem C storage to disturbances and other global change factors, such as nitrogen deposition, land use changes, and altered precipitation. The theoretical framework is simple and straightforward but able to characterize the direction and rate of C storage change, which are arguably among the most critical issues for quantifying terrestrial C sequestration. Future research should explicitly incorporate stochastic disturbance regime shifts (e.g., Weng et al., 2012) and vegetation dynamics (Moorcroft et al., 2001; Purves and Pacala, 2008; Fisher et al., 2010; Weng et al., 2015) into this theoretical framework to explore their theoretical issues related to biogeochemistry.

6 Code availability

Computer code of the TECO model and its physical emulator are available at Yiqi Luo’s website (EcoLab, 2017).

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