

REMARKS ON EXACTNESS NOTIONS PERTAINING TO PUSHOUTS

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ABSTRACT. We call a finitely complete category *diexact* if every difunctional relation admits a pushout which is stable under pullback and itself a pullback. We prove three results relating to diexact categories: firstly, that a category is a pretopos if and only if it is diexact with a strict initial object; secondly, that a category is diexact if and only if it is Barr-exact, and every pair of monomorphisms admits a pushout which is stable and a pullback; and thirdly, that a small category with finite limits and pushouts of difunctional relations is diexact if and only if it admits a full structure-preserving embedding into a Grothendieck topos.

1. Introduction

Amongst the first facts that a category theorist will learn about limits and colimits is that certain limit or colimit types suffice for the construction of other ones. Thus, for example, all small colimits may be constructed from small coproducts and coequalisers, or instead, from finite colimits and filtered ones; whilst finite colimits may in turn be constructed from finite coproducts and coequalisers, or alternatively, from the initial object and pushouts.

Somewhat later, a category theorist becomes cognisant of notions such as regularity, Barr-exactness or extensivity, which involve the existence of finite limits, of certain colimits, and of “exactness conditions” expressing the good behaviour of the colimits with respect to the finite limits. In [4], Lack and the author described how such structures may be recognised as instances of a general theory of cocompleteness, fully the equal of the classical theory, but now existing “in the lex world”; more precisely, in the 2-category **LEX** of finitely complete categories and finite-limit preserving functors.

This paves the way for our studying relative constructibility of exactness notions just as is done for ordinary colimits. The maximal exactness notion is that of being an *infinitary pretopos*, and again this may be constructed from lesser notions in various ways. A category is an infinitary pretopos just when it is infinitary extensive and Barr-exact—thus, having well-behaved coproducts, and well-behaved coequalisers of equivalence relations; alternatively, just when it is a pretopos and admits filtered colimits commuting with finite limits. Now a category is a pretopos just when it is (finitary) extensive and Barr-exact, which is analogous to the construction of finite colimits from finite coproducts and co-

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equalisers; but it is notable that there is no corresponding analogue for the constructibility of finite colimits from pushouts and an initial object.

The purpose of these remarks is to provide such an analogue. We call a finitely complete category *diexact* if it admits pushouts of difunctional (also called Mal'tsev) relations [9], and every such pushout is stable under pullback and itself a pullback square. The “di-” part of the name reminds us we are dealing with *pairs* of maps, which are to be *difunctional* relations; the “-exact” part signifies that the notion is an instance of the framework of [4], meaning that the compatibilities imposed between finite limits and pushouts of difunctional relations in a diexact category are precisely those which hold in any Grothendieck topos. Note that, in particular, the assumption of stability of pushouts is substantive; as observed by Barr [1], the corresponding condition without this clause is validated not only in any topos, but also in any abelian category.

We prove three results relating to diexact categories. The first is the relative constructibility result alluded to above: it says that a category is a pretopos if and only if it is diexact with a strict initial object. The second considers diexactness in the absence of a strict initial object, and shows that this notion is in turn constructible from lesser ones: we prove that a category is diexact just when it is Barr-exact and every pair of monomorphisms admits a pushout which is stable and a pullback; equally, just when it is Barr-exact and adhesive in the sense of [7]. Our third result states that a small category with finite limits and pushouts of difunctional relations is diexact just when it admits a structure-preserving full embedding into a Grothendieck topos. It follows that, as claimed above, diexactness is an exactness notion in the precise sense delineated in [4].

Diexactness involves only *connected* colimits and finite limits, and so is stable under passage to the coslice; so that, for example, the category of pointed sets is diexact, though it is not a pretopos as its initial object is a zero object. The property of having filtered colimits commuting with finite limits is also stable under coslicing, and so also possessed by the category of pointed sets; in fact, we will show in future work that the “**Set**_{*}-enriched Grothendieck toposes”—that is, the **Set**_{*}-categories arising as localisations of presheaf **Set**_{*}-categories—are precisely the locally presentable categories which are diexact, with a zero object, and with filtered colimits commuting with finite limits.

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2. The results

We assume that the reader is familiar with the notions of *regular*, *Barr-exact*, *extensive* and *coherent* category, and of *strict* initial object; they could, for example, consult [6, Section A1]. Recall that a *pretopos* is a finitely complete category which is both extensive and Barr-exact (and thus also coherent). Although a pretopos admits finite coproducts

and coequalisers of equivalence relations, it need not admit all coequalisers; consequently, the general pretopos cannot admit all pushouts, since these, together with the initial object, would imply the existence of all finite colimits. However, a pretopos certainly has *some* pushouts; for example, pushouts over the initial object yielding coproducts. What we aim to describe is a class of well-behaved pushouts which exist in any pretopos, and which, in the presence of a strict initial object, completely characterise the pretoposes.

By a *difunctional relation* in a finitely complete category, we mean a jointly monic span $f: A \leftarrow C \rightarrow B: g$ for which there is a factorisation

$$\begin{array}{ccc}
 & C \times_B C & \times_A C \\
 & \swarrow f \cdot \pi_1 & \downarrow \text{---} \downarrow \\
 & & C \\
 & \swarrow f & \searrow g \\
 A & & B
 \end{array}$$

In the category of sets, a relation $R \subset A \times B$ is difunctional just when it satisfies the condition $(a R b) \wedge (a R b') \wedge (a' R b) \Rightarrow (a' R b')$; a span $h: A \leftarrow C \rightarrow B$ in the general \mathcal{C} is a difunctional relation just when $\mathcal{C}(X, C)$ is a difunctional relation in **Set** for each $X \in \mathcal{C}$. Some important classes of difunctional relations are:

- (i) Any span $f: A \leftarrow C \rightarrow B: g$ in which either f or g is monic;
- (ii) Any span $f: A \leftarrow C \rightarrow B: g$ which is the pullback of a cospan;
- (iii) Any endospan $s: A \leftarrow E \rightarrow A: t$ constituting an equivalence relation on A . Indeed, an endospan is an equivalence relation if and only if it is difunctional and reflexive.

We call a finitely complete category \mathcal{C} *diexact* if it admits pushouts of difunctional relations, and moreover, every such pushout square is stable under pullback and is itself a pullback. Equivalently, a category is diexact if it admits stable pushouts of pullbacks of pairs of arrows, and every difunctional relation is a pullback span.

2.1. PROPOSITION. *A pretopos is diexact.*

Our proof follows that given in [2, Lemma 1.2.4]. As there, we will exploit the locally preordered *bicategory of relations* $\mathbf{Rel}(\mathcal{C})$ associated to a regular category \mathcal{C} ; its objects are those of \mathcal{C} , its morphisms are jointly monic spans in \mathcal{C} and its 2-cells are span morphisms. We write $(-)^o$ for the identity-on-objects involution $\mathbf{Rel}(\mathcal{C})^{\text{op}} \rightarrow \mathbf{Rel}(\mathcal{C})$ that exchanges domain and codomain, and given a morphism $f: A \rightarrow B$ of \mathcal{C} , we will write f also to denote the corresponding relation $1: A \leftarrow A \rightarrow B: f$ in $\mathbf{Rel}(\mathcal{C})$. Recall that, with this convention, we have $f \dashv f^o$ in $\mathbf{Rel}(\mathcal{C})$.

PROOF. Given a difunctional relation $f: A \leftarrow C \rightarrow B: g$ in \mathcal{C} , we let $R = gf^o: A \dashv\vdash B$ be the corresponding morphism in $\mathbf{Rel}(\mathcal{C})$; now difunctionality amounts to the inequality $RR^oR \leq R$. Because \mathcal{C} is coherent, $\mathbf{Rel}(\mathcal{C})$ has finite unions in each hom-preorder, preserved by composition on each side; because \mathcal{C} is moreover extensive, its finite coproducts extend to $\mathbf{Rel}(\mathcal{C})$, there becoming biproducts. As explained in [3, Section 6], this allows

us to use a matrix calculus to describe relations between coproducts, and so we may form the relation

$$E = \begin{pmatrix} 1_A \cup R^\circ R & R^\circ \\ R & 1_B \cup RR^\circ \end{pmatrix} : A + B \rightrightarrows A + B .$$

This is clearly reflexive and symmetric, whilst transitivity $EE \leq E$ follows by multiplying matrices and using $RR^\circ R \leq R$. So E is an equivalence relation on $A + B$, which, since \mathcal{C} is Barr-exact, admits a coequaliser $[h, k]: A + B \rightarrow D$. The universal property of this coequaliser, expressed in terms of $\mathbf{Rel}(\mathcal{C})$, says that $h: A \rightarrow D$ and $k: B \rightarrow D$ are initial amongst maps with

$$(h \ k) \begin{pmatrix} 1_A \cup R^\circ R & R^\circ \\ R & 1_B \cup RR^\circ \end{pmatrix} \leq (h \ k) : A + B \rightrightarrows D .$$

By expanding this condition out, it is easy to see that it is equivalent to the single condition that $kR \leq h$; in other words, that $kgf^\circ \leq h$; in other words, that $kg \leq hf$ in $\mathbf{Rel}(\mathcal{C})$, or in other words, that $kg = hf$ in \mathcal{C} . Thus h and k exhibit D as a pushout of f against g , and in fact as a stable pushout, since the construction used only colimits stable under pullback. Moreover, since \mathcal{C} is Barr-exact, E is the kernel-pair of $[h, k]: A + B \rightarrow D$, so that

$$E = \begin{pmatrix} h^\circ \\ k^\circ \end{pmatrix} (h \ k) : A + B \rightrightarrows A + B$$

in $\mathbf{Rel}(\mathcal{C})$; in particular, we have $k^\circ h = R = gf^\circ: A \rightrightarrows B$, so that C is the pullback of h against k , as required. \blacksquare

We now show that well-behaved pushouts of difunctional relations, together with a strict initial object, serve to completely characterise pretoposes. This gives us the promised analogue ‘‘in the lex world’’ of the construction of all finite colimits from pushouts and the initial object.

2.2. THEOREM. *A finitely complete category \mathcal{C} is a pretopos if and only if it is diexact with a strict initial object.*

PROOF. If \mathcal{C} is a pretopos, then it certainly has a strict initial object, and we have just seen that it is also diexact. Suppose conversely that \mathcal{C} is diexact with a strict initial object. Then for any A and B the unique maps $0 \rightarrow A$ and $0 \rightarrow B$ are monic; whence $A \leftarrow 0 \rightarrow B$ is a difunctional relation, and so admits a stable pushout which is also a pullback. Such a pushout is a stable coproduct of A and B ; that it is also a pullback says that this coproduct is disjoint, so showing that \mathcal{C} is extensive. Now any equivalence relation $(s, t): R \rightrightarrows A$ in \mathcal{C} defines a difunctional relation from A to A , which consequently admits a stable pushout which is also a pullback. Since an equivalence relation is a reflexive pair, this pushout is equally a stable coequaliser of (s, t) ; that it is also a pullback now says that (s, t) is the kernel-pair of its coequaliser, so that \mathcal{C} is Barr-exact. \blacksquare

This result characterises pretoposes in terms of diexactness and a strict initial object. We now examine what happens when we remove the requirement of a strict initial object. In the following result, we call a finitely complete category \mathcal{C} *adhesive*, as in [7], if it admits pushouts along monomorphisms, which are stable and are pullbacks; this is not in fact the definition given in [7], but was shown to be equivalent to it in [5]. We call \mathcal{C} *amalgamable* if every span of monomorphisms admits a pushout which is stable and a pullback.

2.3. THEOREM. *For a finitely complete \mathcal{C} , the following are equivalent:*

- (i) \mathcal{C} is diexact;
- (ii) \mathcal{C} is Barr-exact and adhesive;
- (iii) \mathcal{C} is Barr-exact and amalgamable.

The implication (ii) \Rightarrow (i) of this result is essentially stated as [8, Theorem 5.2], though under the unnecessary additional assumption that \mathcal{C} have all pushouts. Observe also that since pretoposes are Barr-exact by definition, and are known to be amalgamable—see [6, Lemma A1.4.8] for example—this result gives another proof of our Proposition 2.1.

PROOF. The implications (i) \Rightarrow (ii) \Rightarrow (iii) are trivial, since a span with both legs monomorphic certainly has one leg monomorphic, and a span with one leg monomorphic is difunctional; it remains to prove (iii) \Rightarrow (i). Suppose that \mathcal{C} is finitely complete, Barr-exact and amalgamable. It follows that \mathcal{C} admits stable binary unions: for given monomorphisms $A \rightarrow C \leftarrow B$, we may form their intersection $A \cap B$ and the pushout P of the projections $A \leftarrow A \cap B \rightarrow B$; now the stability of this pushout ensures that the induced map $P \rightarrow C$ is monomorphic—see [7, Theorem 5.1], for example—so that P is the stable union of the subobjects A and B . It follows that $\mathbf{Rel}(\mathcal{C})$ admits binary unions in each of its hom-preorders, preserved by composition on both sides.

We first prove that any difunctional relation $f: A \leftarrow C \rightarrow B: g$ in \mathcal{C} with g regular epimorphic admits a stable pushout which is a pullback. Given such a span, we consider the solid part of the diagram

$$\begin{array}{ccccc} M & \xrightarrow{c_0} & C & \xrightarrow{g} & B \\ \downarrow 1 & & \downarrow f & & \downarrow k \\ M & \xrightarrow{fc_0} & A & \xrightarrow{h} & D \end{array},$$

with (c_0, c_1) the kernel-pair of g . Taking $R = gf^o: A \rightarrow B$ in $\mathbf{Rel}(\mathcal{C})$ as before, difunctionality $RR^oR \leq R$ implies that $1_A \cup R^oR$ is an equivalence relation on A . Let $h: A \rightarrow D$ be its coequaliser; so h is initial amongst maps such that $h(1_A \cup R^oR) \leq h$, or equally, such that $hR^oR \leq h$. But $hR^oR = hfg^ogf^o = hfc_0c_1^of^o$, and so h is initial such that $hfc_0 \leq hfc_1$ in $\mathbf{Rel}(\mathcal{C})$, or such that $hfc_0 = hfc_1$ in \mathcal{C} . In other words, h is a coequaliser of (fc_0, fc_1) , and so both rows of the above diagram are coequalisers. Let $k: B \rightarrow D$ be the induced comparison map, as indicated; now because the left-hand vertical map is an identity, the right square is a pushout. This pushout is clearly stable under pullback, having been constructed from stable colimits; to show that it itself is a pullback is equally

to show that $R = k^\circ h$ in $\mathbf{Rel}(\mathcal{C})$. Because g is regular epimorphic, we have $1_B = gg^\circ$ and so $k^\circ h = gg^\circ k^\circ h = gf^\circ h^\circ h = Rh^\circ h$. But because \mathcal{C} is Barr-exact, $h^\circ h = 1_A \cup R^\circ R$ and so $k^\circ h = R(1_A \cup R^\circ R) = R \cup RR^\circ R = R$ as required.

We now prove that \mathcal{C} is diexact. Given a difunctional relation $f: A \leftarrow C \rightarrow B: g$ in \mathcal{C} , form a (regular epi, mono) factorisation $g = g_2 \circ g_1$. It is easy to see that the pair (f, g_1) is again a difunctional relation, which by the case just proved admits a stable pushout and pullback, as on the left in:

$$\begin{array}{ccc} C & \xrightarrow{g_1} \twoheadrightarrow C' & \xrightarrow{g_2} B \\ f \downarrow & & \downarrow f' \\ A & \longrightarrow \twoheadrightarrow & A' \end{array} \qquad \begin{array}{ccc} C' & \xrightarrow{f'_1} \twoheadrightarrow C'' & \xrightarrow{f'_2} A' \\ g_2 \downarrow & & \downarrow g'_2 \\ B & \longrightarrow \twoheadrightarrow & B' \end{array} .$$

Now forming a (regular epi, mono) factorisation $f' = f'_2 \circ f'_1$, we obtain a difunctional relation (f'_1, g_2) which since f'_1 is regular epimorphic, admits a stable pushout and pullback, as on the right above. On pulling back this pushout square along g'_2 , its left edge becomes invertible; since the resultant square is still a pushout, its right edge must also be invertible, which is to say that g'_2 has trivial kernel-pair, and so is monomorphic. So (f'_2, g'_2) is a pair of monomorphisms, which, as \mathcal{C} is amalgamable, admit a stable pushout and pullback. Pasting together the three pushout squares just obtained, we conclude that (f, g) admits a stable pushout and pullback as required. \blacksquare

For our third and final result, we prove an embedding theorem for diexact categories, showing that they capture precisely the compatibilities between finite limits and pushouts of difunctional relations that hold in any Grothendieck topos. It follows from this that diexactness is an exactness notion in the sense of [4].

2.4. THEOREM. *For \mathcal{C} a small, finitely complete category admitting pushouts of difunctional relations, the following are equivalent:*

- (i) \mathcal{C} is diexact;
- (ii) \mathcal{C} admits a full embedding into a Grothendieck topos via a functor preserving finite limits and pushouts of difunctional relations.

PROOF. Any Grothendieck topos is a pretopos, hence diexact; and clearly any full subcategory of a diexact category closed under the relevant limits and colimits will again be diexact. So if $J: \mathcal{C} \rightarrow \mathcal{E}$ is a full embedding of \mathcal{C} into a Grothendieck topos, then the essential image of J is diexact; but \mathcal{C} is equivalent to this essential image, and hence is itself diexact. This shows that (ii) \Rightarrow (i).

Conversely, suppose that \mathcal{C} is diexact. We consider the smallest topology on \mathcal{C} for which every pair of maps $A \rightarrow D \leftarrow B$ arising as the pushout of some difunctional relation is covering. Since such covers are stably effective-epimorphic, they generate a subcanonical topology on \mathcal{C} and now the restricted Yoneda embedding provides a limit-preserving full embedding $J: \mathcal{C} \rightarrow \mathbf{Sh}(\mathcal{C})$. We must show that J also preserves pushouts of difunctional relations; for this, it suffices to show that it preserves coequalisers of equivalence relations

and pushouts of pairs of monomorphisms, since Theorem 2.3 used only these colimits (together with finite limits) to construct pushouts of difunctional relations in a diexact category.

If $(s, t): E \rightrightarrows A$ is an equivalence relation in \mathcal{C} , then its coequaliser $q: A \twoheadrightarrow B$ is a singleton cover, and so Jq is an epimorphism in a topos, hence the coequaliser of its kernel-pair. But that kernel-pair is the image under J of q 's kernel-pair (s, t) , whence J preserves coequalisers of equivalence relations. On the other hand, if $f: A \leftarrow B \rightarrow C: g$ is a pair of monomorphisms in \mathcal{C} , then they admit a pushout $h: A \twoheadrightarrow D \leftarrow C: k$ where, arguing as in the proof of Theorem 2.3, both h and k are monomorphic. Since (h, k) comprise a covering family, (Jh, Jk) are a jointly epimorphic pair of monomorphisms in a topos, and are thus the pushout of their own pullback; but that pullback is the image under J of the pullback of h and k , which is (f, g) . Thus J preserves pushouts of pairs of monomorphisms as well as coequalisers of equivalence relations; and so as argued above, it also preserves pushouts of difunctional relations. ■

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